



Pore-scale reactive transport modeling in cementitious materials: Development and application of a high-performance computing code based on the Lattice-Boltzmann method

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