



## Multi-dimensional GPR full-waveform inversion for small-scale hydrogeophysical soil characterization

Dominik Hoven

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