



Laboratory Course

Neutron Scattering

Lectures

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Reiner Zorn (Editors)

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Shibabrata Nandi, Mirijam Zobel, Reiner Zorn (Editors)

Neutron Scattering

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Th. Brückel

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2 Properties of the neutron

P. Zakalek

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U. Rücker

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High Brilliance Source project group

Forschungszentrum Jülich GmbH

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Shibabrata Nandi

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