



# Quantitative atomic-level investigation of solid materials through multidimensional electron diffraction measurements

Hoelen Laurence Lalandec-Robert

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# Contents

<b>Abstract</b>	<b>vii</b>
<b>Kurzfassung</b>	<b>ix</b>
<b>Acknowledgements</b>	<b>xi</b>
<b>List of publications</b>	<b>xiii</b>
<b>Contributions to conferences</b>	<b>xv</b>
<b>Abbreviations</b>	<b>xvii</b>
<b>Naming conventions</b>	<b>xix</b>
Physical constants . . . . .	xix
Imaging parameters . . . . .	xix
Physical variables . . . . .	xx
Further functions and operators . . . . .	xxi
<b>Introduction</b>	<b>1</b>
Material design at the nanometric scale . . . . .	1
High-resolution scanning transmission electron microscopy . . . . .	2
Contents of this thesis . . . . .	3

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<b>1</b>	<b>Fundamental aspects of TEM</b>	<b>5</b>
	Summary . . . . .	5
1.1	Instrumentation . . . . .	5
1.1.1	Methodological principle . . . . .	5
1.1.2	Magnetic lenses and operation modes . . . . .	6
1.1.3	Electron sources . . . . .	10
1.1.4	Electron detectors . . . . .	14
1.2	Beam-specimen interaction . . . . .	15
1.2.1	Relativistic correction . . . . .	15
1.2.2	Paraxial approximation . . . . .	17
1.2.3	Potential and scattering factors . . . . .	18
1.2.4	Multislice solution . . . . .	19
1.2.5	Numerical sampling . . . . .	21
1.2.6	Thin specimen approximations . . . . .	22
1.3	Optical aspects of STEM . . . . .	23
1.3.1	Lateral resolution for a diffraction-limited system . . . . .	23
1.3.2	Optical aberrations . . . . .	24
1.3.3	Depth of focus . . . . .	26
1.3.4	Principle of reciprocity under the phase object approximation . . . . .	27
1.4	Role of wave coherence and energy-loss . . . . .	29
1.4.1	Partial coherence and the density matrix . . . . .	29
1.4.2	Spatial and temporal incoherence of the illumination . . . . .	31
1.4.3	Lattice vibrations and phonon excitation . . . . .	32
1.4.4	Inelastic scattering . . . . .	34
1.4.5	Channelling dynamics in quasi-elastic conditions . . . . .	35

---

1.4.6	Specimen damage and electron dose . . . . .	37
	Discussion . . . . .	38
<b>2</b>	<b>Imaging modes in STEM and processing of four-dimensional data</b>	<b>39</b>
	Summary . . . . .	39
2.1	Imaging modes in STEM and CTEM . . . . .	39
2.1.1	Momentum-resolved STEM . . . . .	39
2.1.2	CTEM imaging and phase contrast . . . . .	42
2.1.3	Conventional STEM . . . . .	43
2.1.4	Z-contrast . . . . .	44
2.1.5	First moment $\langle \vec{q} \rangle$ and differential phase contrast . . . . .	47
2.1.6	Analysis based on multiple micrographs . . . . .	50
2.2	Self-consistent calibration of diffraction coordinates . . . . .	52
2.2.1	Mapping of reciprocal space in the presence of elliptical distortion . . . . .	52
2.2.2	Correction of the rotation error . . . . .	54
2.2.3	Signal extraction by virtual detectors . . . . .	55
2.3	Calculation, derivation and integration of the first moment $\langle \vec{q} \rangle$ . . . . .	56
2.3.1	Extraction from the MR-STEM data . . . . .	56
2.3.2	Iterative finite differences . . . . .	56
2.3.3	Fourier integration . . . . .	57
2.4	Scalar second moment $\langle q^2 \rangle$ . . . . .	58
2.4.1	Calculation of $\langle q^2 \rangle$ in diffraction space . . . . .	58
2.4.2	Prediction of convergence properties by Mott scattering . . . . .	61
2.4.3	Verification by multislice simulation . . . . .	62
	Discussion . . . . .	64

---

<b>3 Influence of plasmon scattering on low-angle electron diffraction</b>	<b>67</b>
Summary . . . . .	67
3.1 Importance of inelastic scattering for momentum-resolution . . . . .	67
3.2 Energy-filtered MR-STEM of Pt in [110] orientation . . . . .	68
3.2.1 Experimental set-up . . . . .	68
3.2.2 Determination of a common interval of thickness . . . . .	70
3.2.3 Results and analysis . . . . .	71
3.3 Multislice simulation model including single plasmon-losses . . . . .	74
3.4 Role of multiple plasmon excitation . . . . .	75
3.5 EF-MR-STEM employing multiple energy windows . . . . .	76
3.5.1 Experimental set-up . . . . .	76
3.5.2 Measurement of incident electron intensity emitted by a CFEG . . . . .	77
3.5.3 Results and analysis . . . . .	79
3.6 Convolutional model for the inclusion of plasmon scattering . . . . .	80
3.6.1 Concept and implementation . . . . .	80
3.6.2 Verification through a simulation . . . . .	81
3.6.3 Application to the experimental data . . . . .	82
Discussion . . . . .	82
<b>4 Focus-dependence of STEM signals and prospects for surface detection</b>	<b>89</b>
Summary . . . . .	89
4.1 Limitations of conventional depth sectioning approaches . . . . .	89
4.2 Case study on $\alpha$ -In <sub>2</sub> Se <sub>3</sub> . . . . .	90
4.2.1 Experimental set-up . . . . .	90
4.2.2 Results and analysis . . . . .	91

---

4.3	Interpretation of experimental results through simulation . . . . .	92
4.3.1	Simulation parameters and focus-dependences . . . . .	92
4.3.2	C-STEM signals . . . . .	94
4.3.3	MR-STEM-specific signals . . . . .	95
4.3.4	Role of acceptance angle in the behavior of $\langle q^2 \rangle$ . . . . .	96
4.3.5	Inversion of $\langle \vec{q} \rangle$ across the focus axis . . . . .	98
4.4	Multislice simulation of bulk Au . . . . .	98
4.5	Surface retrieval using a focal series . . . . .	99
4.6	Focus-dependence for different depths of focus . . . . .	104
4.7	Role of geometrical aberrations . . . . .	105
4.7.1	Third-order spherical aberration . . . . .	105
4.7.2	First-order astigmatism . . . . .	106
4.7.3	Second-order coma and astigmatism . . . . .	107
4.8	Influence of the partial spatial and temporal coherence . . . . .	107
4.9	Other factors relating to the specimen . . . . .	108
4.9.1	Specimen tilt . . . . .	108
4.9.2	Carbon contamination . . . . .	109
4.9.3	Temperature . . . . .	110
4.10	Comparison with other materials . . . . .	111
	Discussion . . . . .	112
	<b>General discussion</b> . . . . .	<b>115</b>
	Scalar second moment $\langle q^2 \rangle$ . . . . .	115
	Role of inelastic scattering in dynamical electron diffraction . . . . .	115
	Influence of probe focus on a variety of MR-STEM signals . . . . .	116

<b>Conclusion</b>	<b>119</b>
<b>Prospects</b>	<b>121</b>
Topography mapping and quantitative analysis via focal series . . . . .	121
Imaging of weakly scattering and dose-sensitive objects . . . . .	121
Shape sensitivity in first moment STEM . . . . .	122
New detectors for the direct measurement of momentum transfer . . . . .	123
<b>Bibliography</b>	<b>125</b>



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