



# Gradient-Free Optimization of Artificial and Biological Networks using Learning to Learn

Alper Yeğenoğlu

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