



# **Computational study of structural and optical properties of two-dimensional transition-metal dichalcogenides with implanted defects**

Stefan Hermann Rost

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