



# High-Performance Computing Approach to Hybrid Functionals in the All-Electron DFT Code FLEUR

Matthias Redies

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