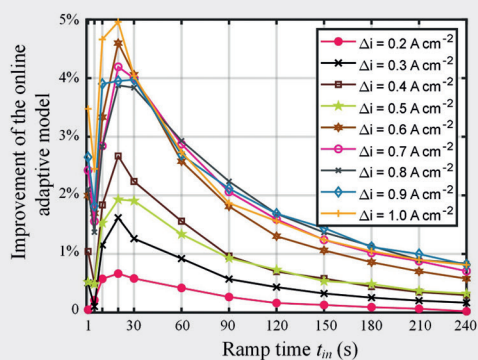
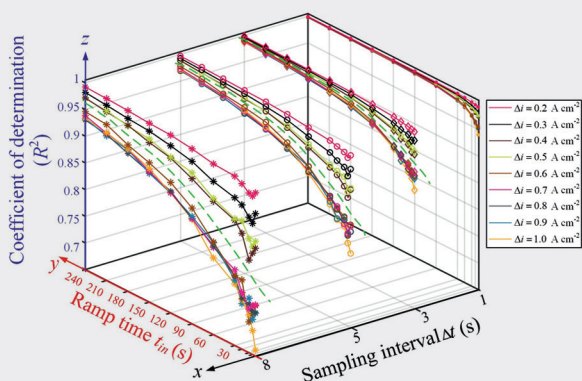
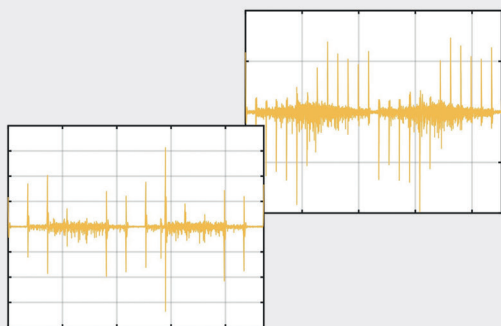
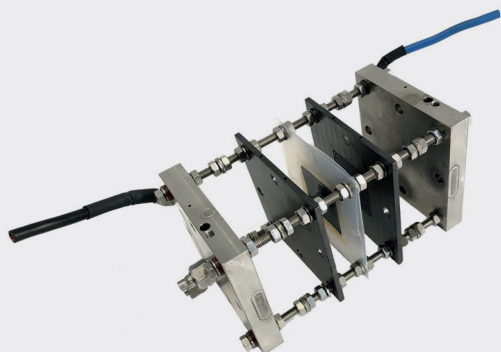




# Machine Learning in Modeling of the Dynamics of Polymer Electrolyte Fuel Cells

Wei Zou

Energie & Umwelt / Energy & Environment

Band / Volume 560

ISBN 978-3-95806-601-4

Forschungszentrum Jülich GmbH  
Institut für Energie- und Klimaforschung  
Elektrochemische Verfahrenstechnik (IEK-14)

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Schriften des Forschungszentrums Jülich  
Reihe Energie & Umwelt / Energy & Environment

Band / Volume 560

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ISSN 1866-1793

ISBN 978-3-95806-601-4

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ISBN 978-3-95806-601-4