



## Complex magnetism of nanostructures on surfaces: from orbital magnetism to spin excitations

Sascha Brinker

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