



# **Towards a Generalized Framework for the Analysis of Solar Cell Performance based on the Principle of Detailed Balance**

Beatrix Johanna Blank

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