



# High spatial resolution and three-dimensional measurement of charge density and electric field in nanoscale materials using off-axis electron holography

Fengshan Zheng

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