



First-principles study of collective spin excitations in noncollinear magnets

Flaviano José dos Santos

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