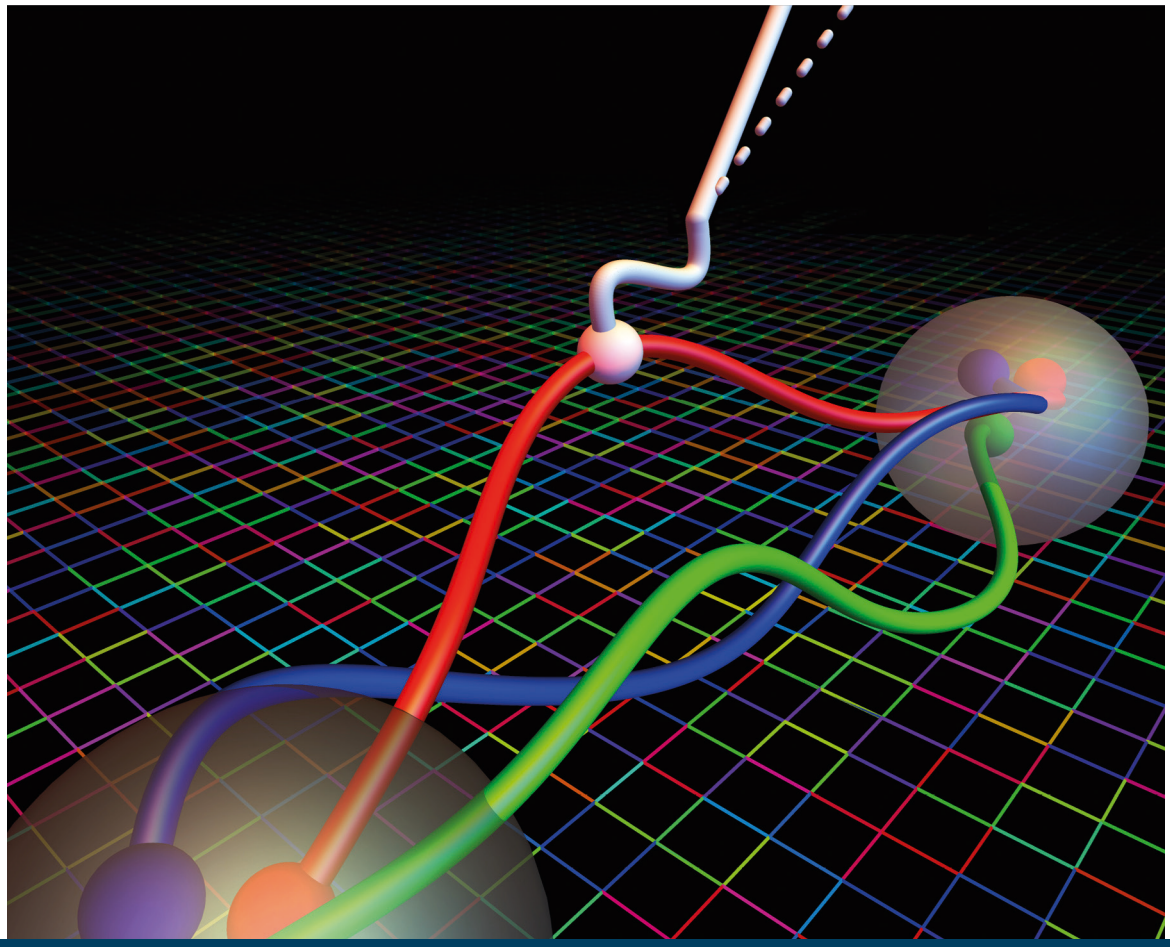

A lattice QCD study of nucleon structure with physical quark masses

Nesreen Hasan

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