



$$G = G^r + G^r \Delta t G$$

$$E_{\text{atom}} = - \sum_{ij} J_{ij} \mathbf{m}_i \cdot \mathbf{m}_j + \sum_{ij} \mathbf{D}_{ij} \cdot (\mathbf{m}_i \times \mathbf{m}_j)$$

## Large-scale Investigations of Non-trivial Magnetic Textures in Chiral Magnets with Density Functional Theory

Marcel Bornemann

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# Contents

<b>1. Introduction</b>	<b>9</b>
<b>2. Density Functional Theory</b>	<b>15</b>
2.1. Born-Oppenheimer Approximation . . . . .	15
2.2. Hohenberg-Kohn Theorems . . . . .	16
2.3. Kohn-Sham Equation . . . . .	16
2.4. Spin Density Functional Theory . . . . .	17
2.5. Exchange-correlation Potential . . . . .	19
<b>3. KKR-Green Function Method</b>	<b>21</b>
3.1. Properties of Green Functions . . . . .	22
3.2. Single-Site Scattering . . . . .	25
3.3. Multiple-Site Scattering . . . . .	28
3.4. Full-potential Treatment . . . . .	31
3.5. Screened KKR Method . . . . .	32
3.6. Self-consistent Solution . . . . .	33
<b>4. Linear-scaling KKR<sub>nano</sub> and High Performance Computing</b>	<b>35</b>
4.1. Iterative Solution of the Dyson Equation . . . . .	36
4.2. Truncation for Linear Scaling . . . . .	39
4.3. Parallelization for High Performance Computing . . . . .	40
4.3.1. Hardware Architectures . . . . .	41
4.3.2. Parallelization Schemes in KKR <sub>nano</sub> . . . . .	44
4.3.3. TFQMR Solver on GPUs . . . . .	49
4.3.4. Benchmarks on Blue Gene/Q . . . . .	53
<b>5. Methodological Improvements to KKR<sub>nano</sub></b>	<b>59</b>
5.1. Non-collinear Magnetism in KKR . . . . .	59
5.2. Relativistic Full-potential Treatment . . . . .	62
5.2.1. Dirac Equation . . . . .	63
5.2.2. Scalar-relativistic Approximation . . . . .	64
5.2.3. Spin-orbit Coupling . . . . .	67
5.2.4. Results for IrMn <sub>3</sub> . . . . .	70
5.3. Generalized Gradient Approximation (GGA) . . . . .	71
5.4. Lloyd's Formula . . . . .	76
5.5. Semi-core Contour . . . . .	81

<b>6. Atomistic Spin Dynamics</b>	<b>83</b>
6.1. Landau-Lifshitz-Gilbert Equation	83
6.2. The Magnetic Hamiltonian	85
6.3. Extraction of Magnetic Interaction Parameters from KKR	87
<b>7. Magnetic Textures in B20 Compounds</b>	<b>89</b>
7.1. Basic Properties of MnGe	90
7.1.1. High-spin/Low-spin Transition	92
7.1.2. Magnetocrystalline Anisotropy	94
7.2. Magnetic Model for MnGe	99
7.2.1. Micromagnetic Parameters	99
7.2.2. Atomistic Spin Dynamics Results	107
7.3. Large-Scale KKRnano Calculations for MnGe	112
7.3.1. Helical Spiral (1Q), Hedgehog Lattice (3Q) and Bloch Point (BP) State	112
7.3.2. Layers	117
7.3.3. $P2_13$ vs. $P2_12_12_1$ Space Group	118
7.4. $Mn_{1-x}Fe_xGe$ Alloys	121
7.4.1. Magnetic Parameters	121
7.4.2. Bloch Point State	126
<b>8. Conclusions</b>	<b>129</b>
<b>A. Appendix</b>	<b>131</b>
A.1. Equation of Motion for Spin Densities in a Magnetic Field	131
<b>Bibliography</b>	<b>133</b>

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