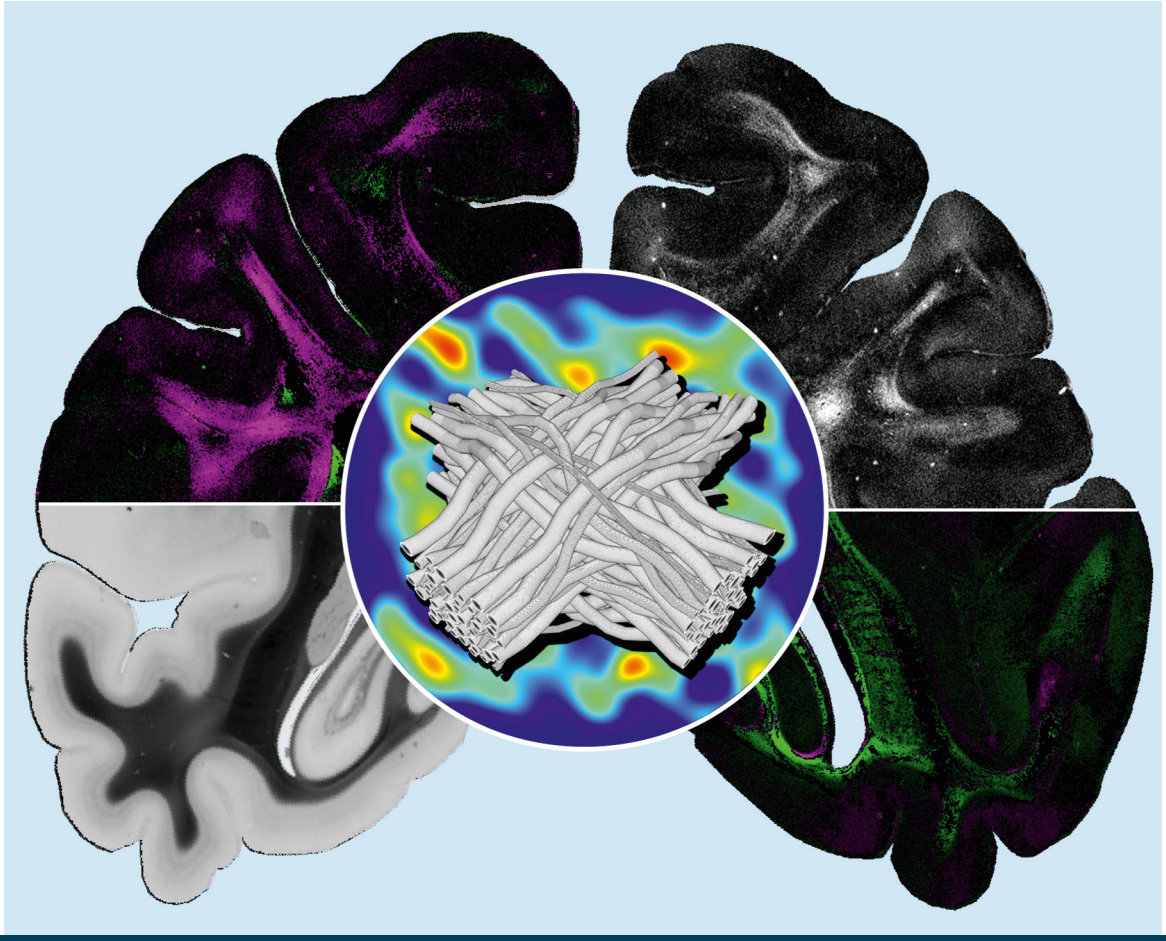

Finite-Difference Time-Domain Simulations Assisting to Reconstruct the Brain's Nerve Fiber Architecture by 3D Polarized Light Imaging

Miriam Menzel

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