



Topological properties of complex magnets from an advanced *ab-initio* Wannier description

Jan-Philipp Hanke

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