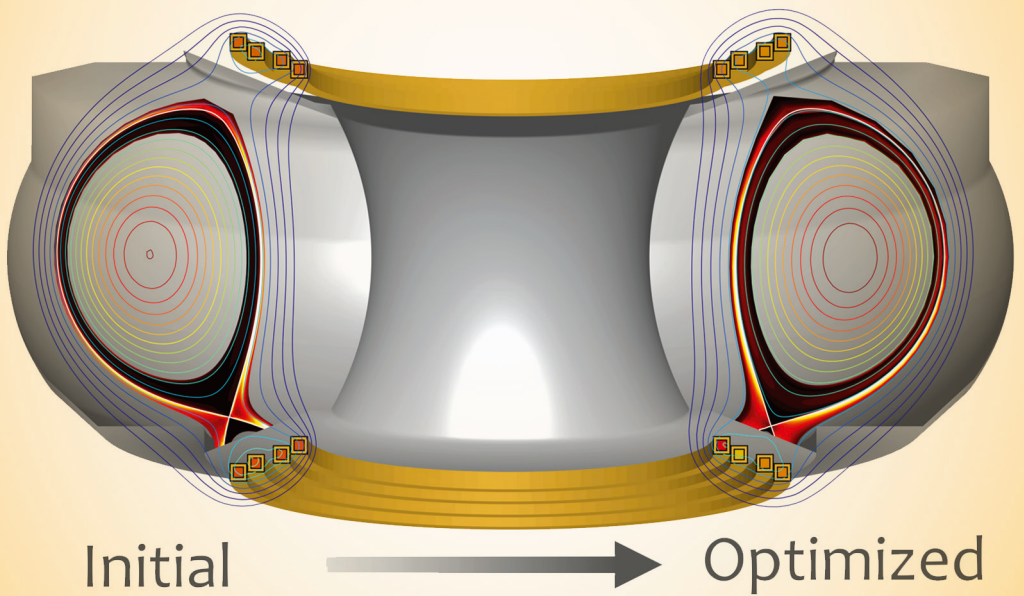


Automated Magnetic Divertor Design for Optimal Power Exhaust

Maarten Blommaert



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Contents

List of Figures	x <i>i</i>
List of Tables	x <i>iii</i>
List of Symbols	xv
1 Introduction	1
1.1 Nuclear fusion: confining the energy of stars	1
1.2 The divertor: a tokamak exhaust system	5
1.2.1 Why today’s tokamaks are equipped with divertors	6
Impurity transport	6
Pumping	7
New plasma and divertor regimes	8
Power exhaust limitations	9
1.2.2 How to prevent excessive target erosion in DEMO?	10
1.3 Computational divertor design	12
1.4 Optimal design	14
1.5 Goals and outline of the thesis	16
2 Optimal Magnetic Divertor Design	21
2.1 Divertor design as an optimization problem	21
2.1.1 First order necessary conditions for optimality	23
2.1.2 Gradient calculation	26
The forward approach to gradient calculation	26
The adjoint approach to gradient calculation	27
Discretization and adjoint approaches	28

CONTENTS

2.2	Optimization algorithms	31
2.2.1	Nested optimization methods	32
2.2.2	SQP, rSQP and one-shot methods	33
2.3	Globalization	35
2.4	Summary	36
3	Integral Magnetic Divertor Model	39
3.1	Magnetic field modelling	41
3.1.1	Quasi-static magnetic field equations	41
3.1.2	Exploiting toroidal (quasi-)symmetry	42
3.1.3	Towards a free boundary equilibrium problem	44
3.1.4	A simple and fast perturbation approach	45
3.2	Plasma edge grid generation	48
3.2.1	Continuous	49
3.2.2	Discrete	52
3.3	Plasma edge modelling	55
3.3.1	Plasma model equations	55
	Ion continuity equation	55
	Ion parallel momentum equation	56
	Neutral pressure diffusion equation	57
	Total internal energy equation	57
	Rate coefficients, radiative loss function and transport co- efficients	58
	Remarks on the model choice	59
3.3.2	Plasma model equations in convection-diffusion form . . .	59
3.3.3	Boundary conditions	61
	Target boundaries	61
	Core boundary	62
	Wall and private flux boundaries	63
3.3.4	Discretizing and solving the plasma edge equations	64
	Solving a correction equation	64
	Boundary conditions	65
3.4	Conclusions	66

4	Automated Design of a JET Configuration	67
4.1	A suitable objective functional formulation	68
4.2	Introducing a core shape constraint	72
4.3	Projection onto the design constraints	74
4.4	Solving the optimization problem	75
4.5	Automated design procedure applied to a JET configuration . . .	78
4.5.1	Test case specification	78
4.5.2	Results	81
	Optimization with low wall heating penalty	81
	Optimization with high wall heating penalty	84
4.6	Conclusion	85
5	In-Parts Adjoint Sensitivities for Efficient Magnetic Divertor Design	89
5.1	Motivation	90
5.2	A problem-adapted efficient computation of the objective gradient	92
5.3	Introducing the continuous adjoint plasma edge model	95
5.3.1	Linearization	96
5.3.2	Integration by parts	97
5.3.3	Adjoint boundary conditions	99
5.4	Derivation of a semi-discrete approach to in-parts adjoint sensitivity calculation	100
	Towards a semi-discrete approach to sensitivity calculation	101
	Finding the correct boundary multipliers	102
5.5	Sensitivity verification with a grid refinement study	105
5.6	Application to optimal current design	107
5.7	Conclusions	111
6	Integration of Free-Boundary Equilibrium Magnetic Model	113
6.1	CEDRES++ free-boundary equilibrium calculations	115
6.2	Comparison of magnetic models	118
6.2.1	Analysis of model assumptions	118
6.2.2	Comparison of sensitivities	121

CONTENTS

6.3	Adapting the FBE calculations for automated target heat load evaluations	125
6.3.1	Estimation of contour line errors	125
6.3.2	Introducing adaptive grid refinement	127
6.4	Sensitivity calculation and verification	128
6.4.1	Test case description	129
6.4.2	Sensitivity calculation and results	130
6.4.3	Setting up design constraints	133
6.4.4	Optimal design results	135
6.5	Conclusions	138
7	One-shot Optimization	141
7.1	Literature review on one-shot approaches	143
7.2	A first attempt to one-shot magnetic divertor design	146
7.2.1	One-shot approach	146
7.2.2	Set-up of an unconstrained WEST test case	147
7.2.3	Discussion of first results	148
7.3	Acceleration of the one-shot procedure	153
7.3.1	Grid deformation method	154
7.3.2	Adapted test case	159
7.3.3	Results and discussion	160
	Convergence behaviour	160
	Optimization efficiency	160
	Conclusions	163
7.4	A novel one-shot strategy with a practical augmented Lagrangian globalization	165
7.4.1	One-shot optimization using a doubly augmented Lagrangian function	166
	Optimization with fixed-point solvers	166
	Doubly augmented Lagrangian theory	168
	Discussion	170
7.4.2	Derivation of a practical augmented Lagrangian merit function	171

CONTENTS

Considerations on the adjoint feasibility penalty	171
A practical augmented Lagrangian merit function	172
7.4.3 A simple line search procedure for globalization	174
7.4.4 A robust approach to Hessian estimation	175
7.5 Application of the globalized one-shot method to the unconstrained test problem	177
7.5.1 From theory to practice	178
7.5.2 Notes on sensitivity calculation	179
7.5.3 Overview of the applied one-shot algorithm	180
7.5.4 Results	181
7.6 One-shot optimization for constrained magnetic divertor design .	185
7.6.1 Constrained one-shot optimization based on an active set strategy	186
7.6.2 Globalization of the constrained one-shot method	190
7.7 Discussion and conclusions	190
8 Discussion and Conclusions	193
8.1 General conclusions	193
Modelling and magnetic divertor designs	194
Development of optimal design algorithms	195
8.2 Suggestions for further research	197
Bibliography	201

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