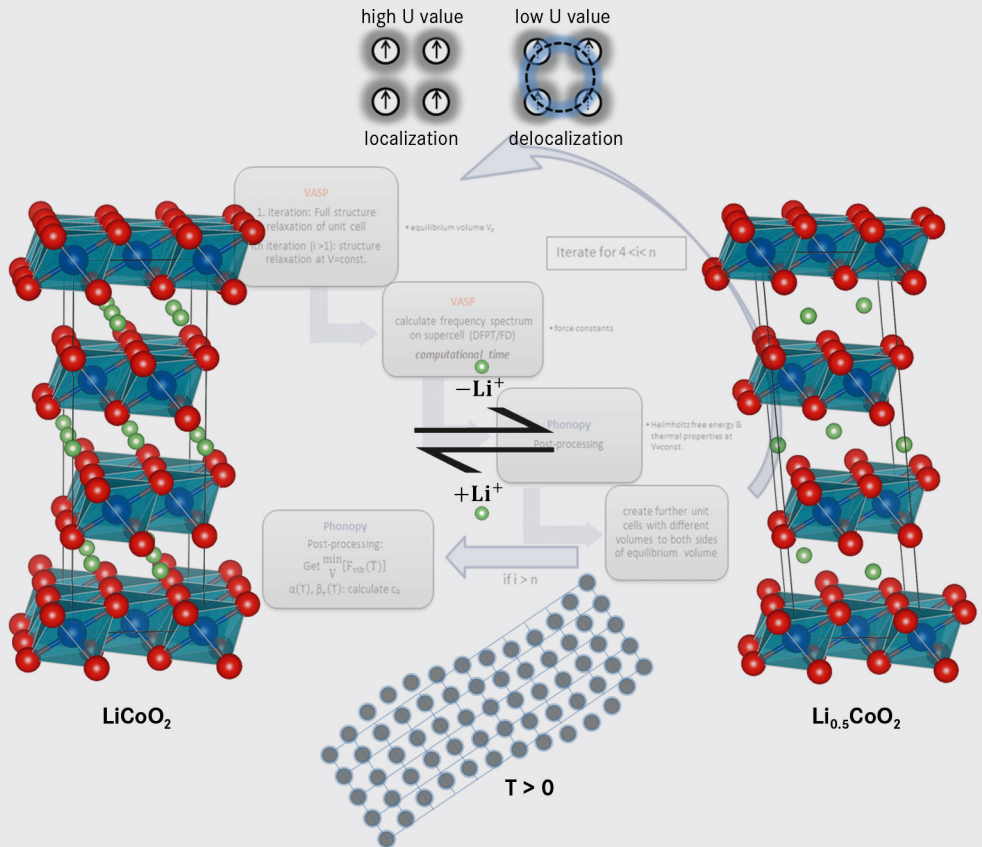


# Modelling Thermodynamic Properties of Intercalation Compounds for Lithium Ion Batteries

Siaufung Oliver Dang



Forschungszentrum Jülich GmbH  
Institute of Energy and Climate Research (IEK)  
Microstructure and Properties of Materials (IEK-2)

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