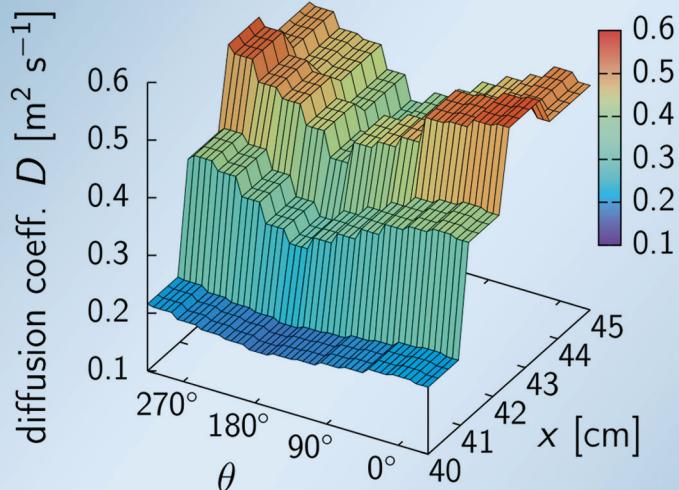


Development and Application of a Multiscale Model for the Magnetic Fusion Edge Plasma Region

Felix Martin Michael Hasenbeck



$$\frac{\partial n_0}{\partial t} + \nabla \cdot [n_0 \mathbf{u}_{||0} - D(\langle \tilde{n} \mathbf{v}_E \rangle) \nabla_{\perp} n_0] = S_{0in}^{ic}$$

$$\begin{aligned} \left(\frac{\partial}{\partial t} + \mathbf{v}_E \cdot \nabla_{\perp} \right) \tilde{n} &= -\mathbf{v}_E \cdot \nabla_{\perp} n_0 + \frac{T_{0e}}{e} \mathcal{K}(\tilde{n}) \\ &- n_0 \mathcal{K}(\phi) - n_0 B_0 (\nabla_{||0} + \tilde{\nabla}_{||}) \left(\frac{u_{||}}{B_0} - \frac{j_{||}}{en_0 B_0} \right) + \gamma(\tilde{n}) \end{aligned}$$

Energie & Umwelt /
Energy & Environment
Band / Volume 307
ISBN 978-3-95806-120-0

Forschungszentrum Jülich GmbH
Institute of Energy and Climate Research
Plasma Physics IEK-4

Development and Application of a Multiscale Model for the Magnetic Fusion Edge Plasma Region

Felix Martin Michael Hasenbeck

Schriften des Forschungszentrums Jülich
Reihe Energie & Umwelt / Energy & Environment

Band / Volume 307

ISSN 1866-1793

ISBN 978-3-95806-120-0

Contents

1. Introduction	11
2. Generic multiscale model for a fluid	15
2.1. From a kinetic to a fluid description	16
2.2. Generic multiscale model equations	20
2.2.1. Scale separation assumption and Reynolds decomposition	21
2.2.2. Particle balance	23
2.2.3. Momentum balance	26
2.2.4. Energy balance	27
2.2.5. Discussion of the generic multiscale model	28
2.3. Outline of a coupled code system	28
2.3.1. Structure of the coupling procedure	29
2.3.2. Averages of temporal and spatial derivatives	36
2.3.3. Macroscale transport models for averaged mesoscale terms . . .	38
2.3.4. Stationary states in the generic multiscale model	39
3. Large scale model for the plasma edge	43
3.1. The tokamak device	44
3.2. Braginskii closure for a collisional, magnetized plasma	47
3.3. The large scale model	52
3.3.1. Assumptions of the large scale edge model	52
3.3.2. Specification of the macroscale transport model	55
3.3.3. Model equations of the self-contained large scale edge model .	56
3.4. Discussion of the large scale model	57
4. Drift fluid models for the plasma edge	59
4.1. Perpendicular fluid drifts	60
4.2. Global drift fluid model	61
4.2.1. Model assumptions	62
4.2.2. Particle balance	63
4.2.3. Total parallel momentum balance	64
4.2.4. Ion and electron energy balance	65
4.2.5. Ohm's law	66
4.2.6. Vorticity equation	67
4.2.7. Discussion of the global drift fluid model	67

4.3.	Local drift fluid model	68
4.3.1.	Assumptions of the local drift fluid model	69
4.3.2.	Local drift fluid model equations	71
5.	Specific multiscale model for the plasma edge	75
5.1.	Model equations	75
5.1.1.	Macroscale part	75
5.1.2.	Mesoscale part	77
5.2.	Discussion of the multiscale model	78
5.3.	Survey on comparable models	78
6.	Macroscale transport models for averaged mesoscale dynamics	81
6.1.	Representation of transport via a diffusion-convection scheme	82
6.1.1.	Fick's laws and drift-diffusion equations	82
6.1.2.	Splitting flux into a diffusive and a convective part	84
6.2.	Passive scalar system	87
6.2.1.	Outline of the passive scalar system	87
6.2.2.	Diffusion in passive scalar simulations for high and low Kubo numbers	89
6.2.3.	Simple coupled code example for the diffusion of passive scalars	100
7.	Example of a 1D coupled code system	105
7.1.	Setup of the coupled code system	106
7.1.1.	Macroscale part: 1D code	106
7.1.2.	Mesoscale part: drift fluid code ATTEMPT	108
7.1.3.	Coupling procedure	110
7.1.4.	Determination of the averaged mesoscale terms	114
7.2.	Comparison of local and non-local ATTEMPT simulations	120
7.3.	Results of the coupled code system	125
7.3.1.	Setup of the simulations	125
7.3.2.	Agreement of the coupled code simulations with the reference simulation	128
7.3.3.	Performance of the procedure to check for the average mesoscale flux	133
7.3.4.	Time savings of the coupled code system	137
7.3.5.	Additional studies	142
7.3.6.	Summary and discussion of results	143
8.	Simulations with the B2-ATTEMPT coupled code system	147
8.1.	Multiscale model of the B2-ATTEMPT system	148
8.2.	Outline of the 2D coupling procedure	150
8.3.	Results of the 2D coupled code system	153
8.3.1.	Assessment of different macroscale transport models	162

8.3.2. Poloidal variation of transport coefficients	164
8.3.3. Summary and conclusions	167
9. Conclusions and Outlook	169
A. Sampling the velocity field for the passive scalar system	175
B. Reference figures of B2-EIRENE simulations	179
References	181
Acknowledgements	191

**Energie & Umwelt/
Energy & Environment
Band / Volume 307
ISBN 978-3-95806-120-0**

