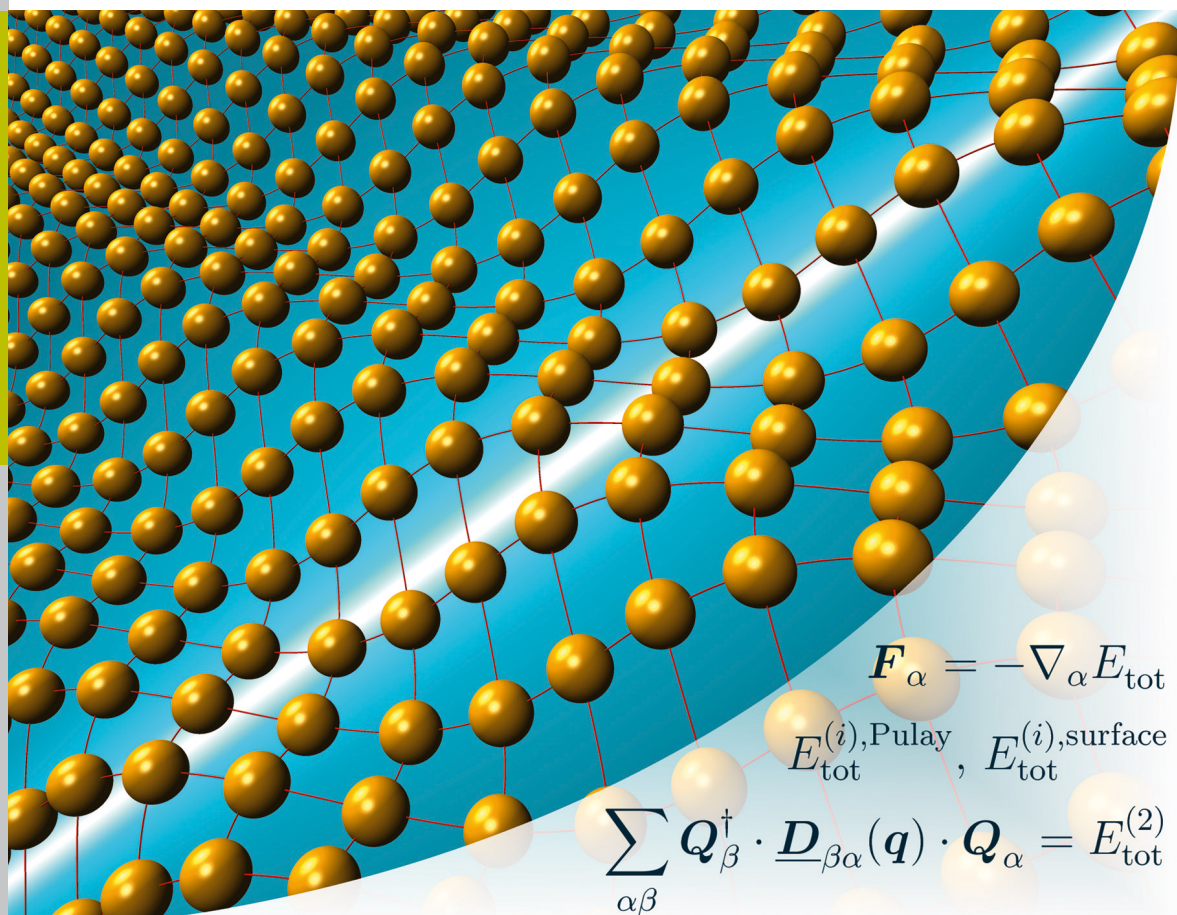


First-principle investigation of displacive response in complex solids

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