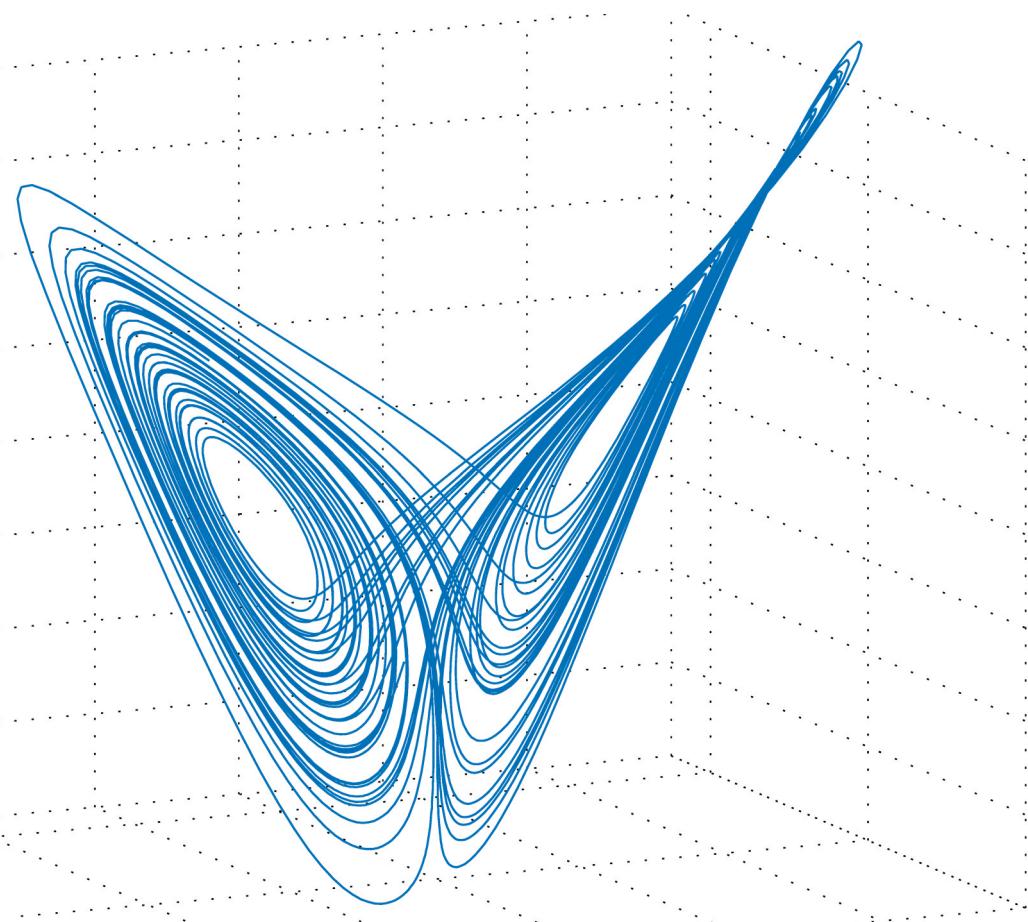


# Model-based Algorithm Development with Focus on Biosignal Processing

Yu Yao

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