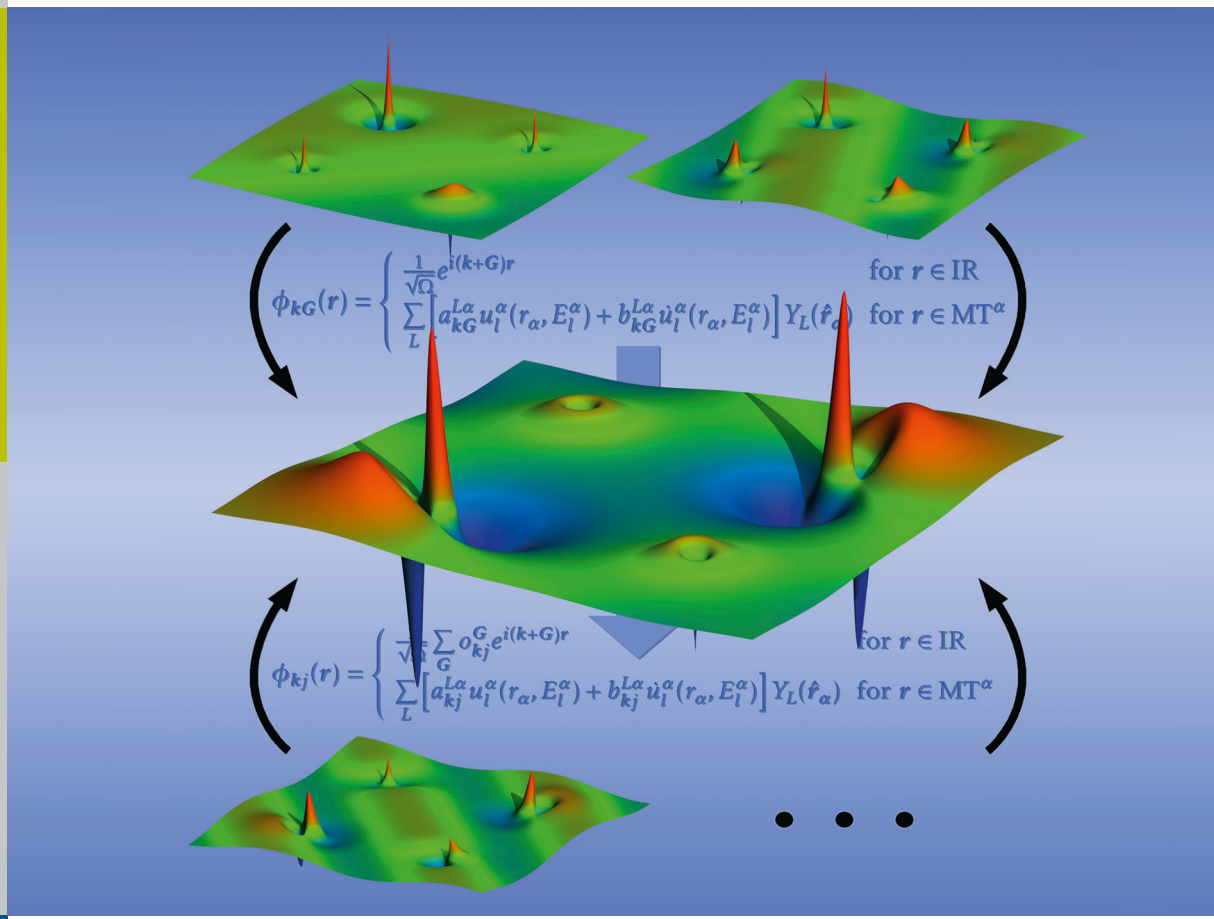
Extending the precision and efficiency of the all-electron full-potential linearized augmented plane-wave density-functional theory method

Gregor Michalicek



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