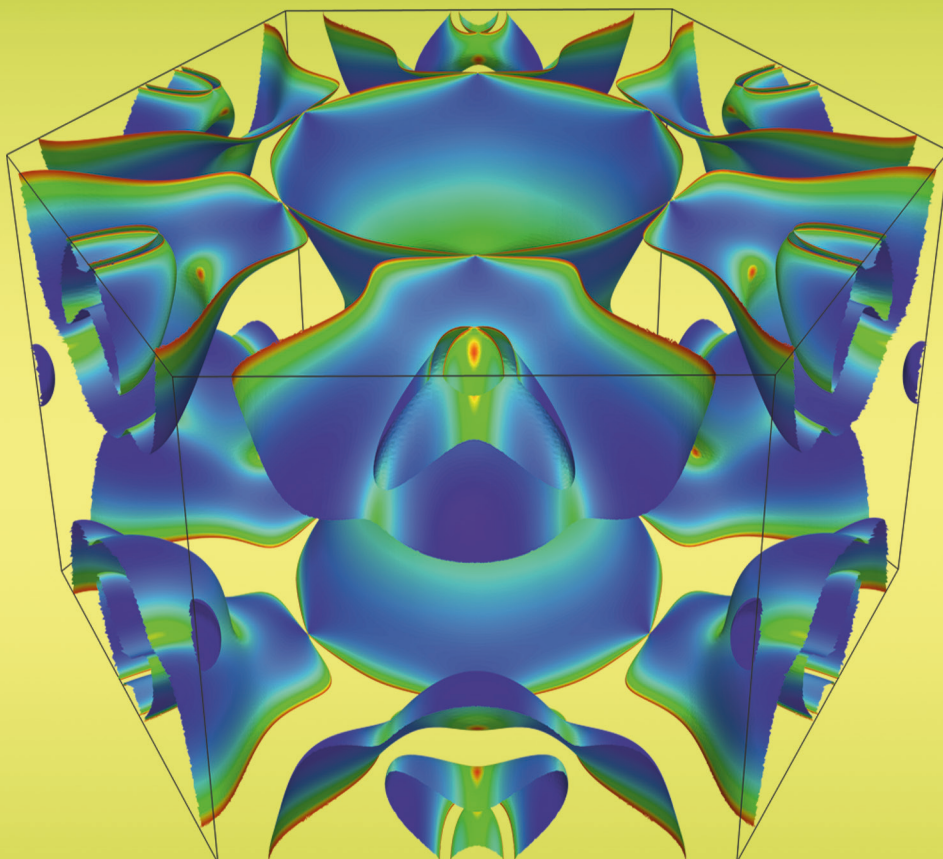




## ***Ab initio* description of transverse transport due to impurity scattering in transition-metals**

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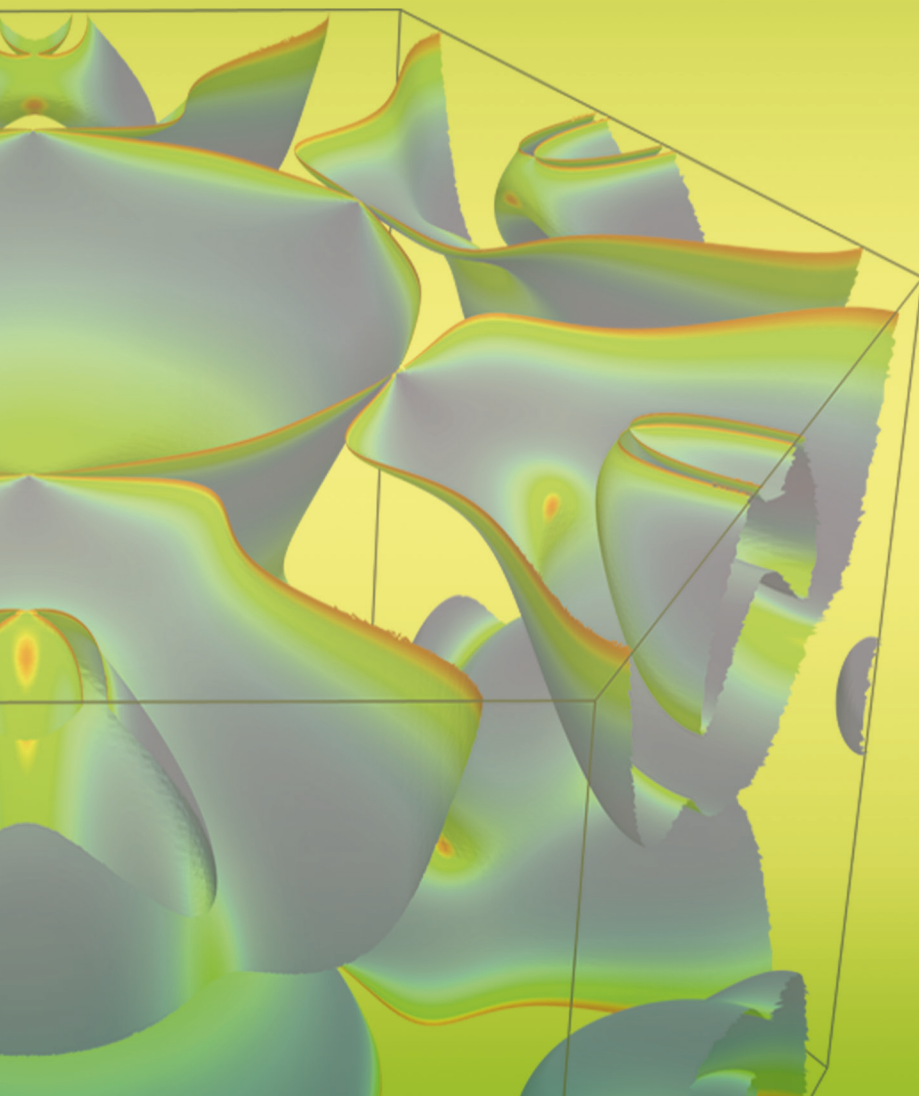
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