

## Interdomain Functional Dynamics of Phosphoglycerate Kinase Studied by Single-Molecule FRET

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# **Interdomain Functional Dynamics of Phosphoglycerate Kinase Studied by Single-Molecule FRET**

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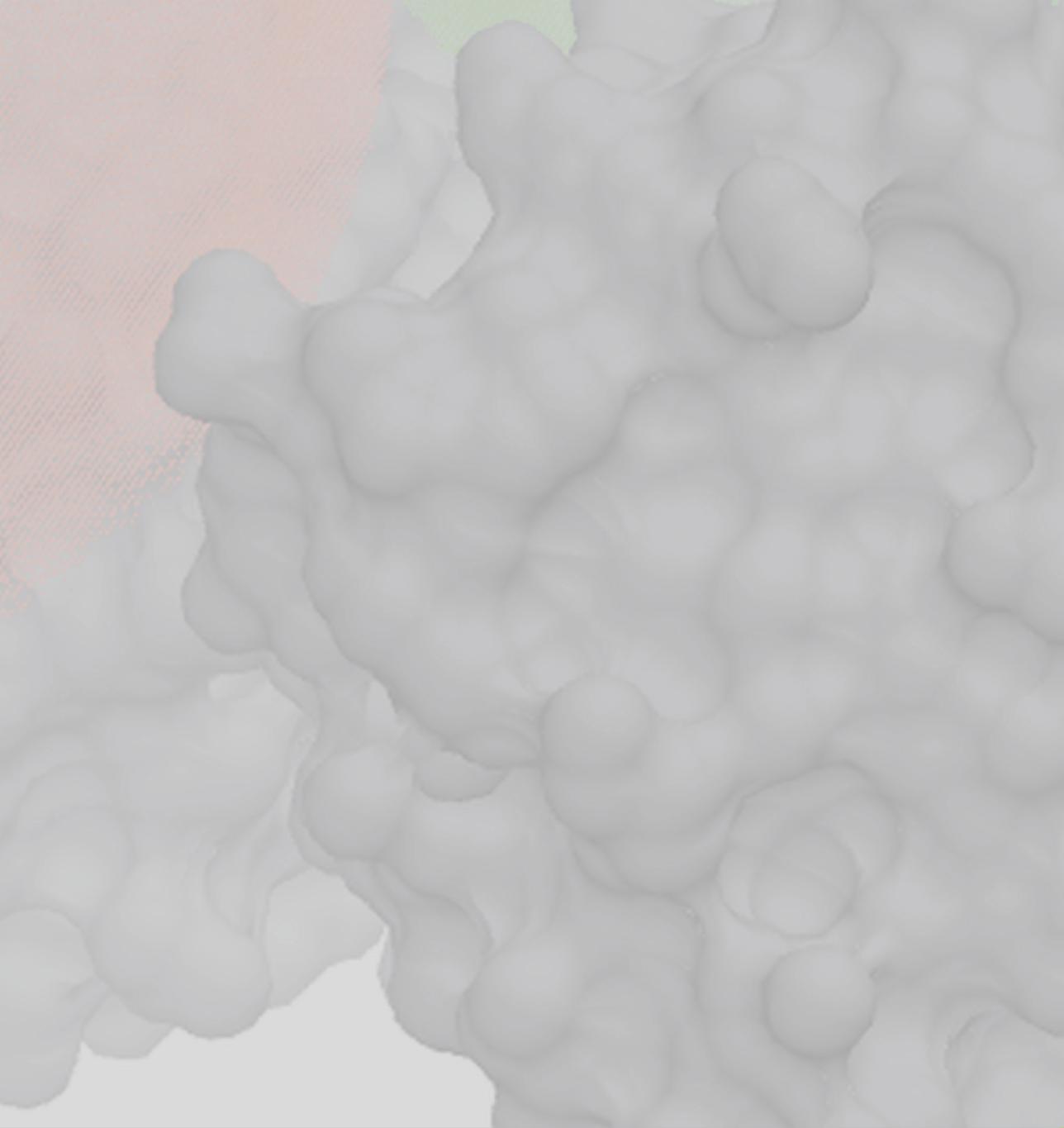
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The top half of the image features a complex, three-dimensional molecular model. The structure is composed of numerous interconnected spheres and rods, rendered in a light gray color. The spheres vary in size and are arranged in a way that suggests a highly branched or porous network. The background behind the model is a gradient of light gray, with a subtle orange and green pattern in the upper left corner. The overall appearance is that of a scientific visualization of a material's atomic or molecular structure.

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