

**Orbital-dependent exchange-correlation functionals in
density-functional theory realized by the FLAPW method**

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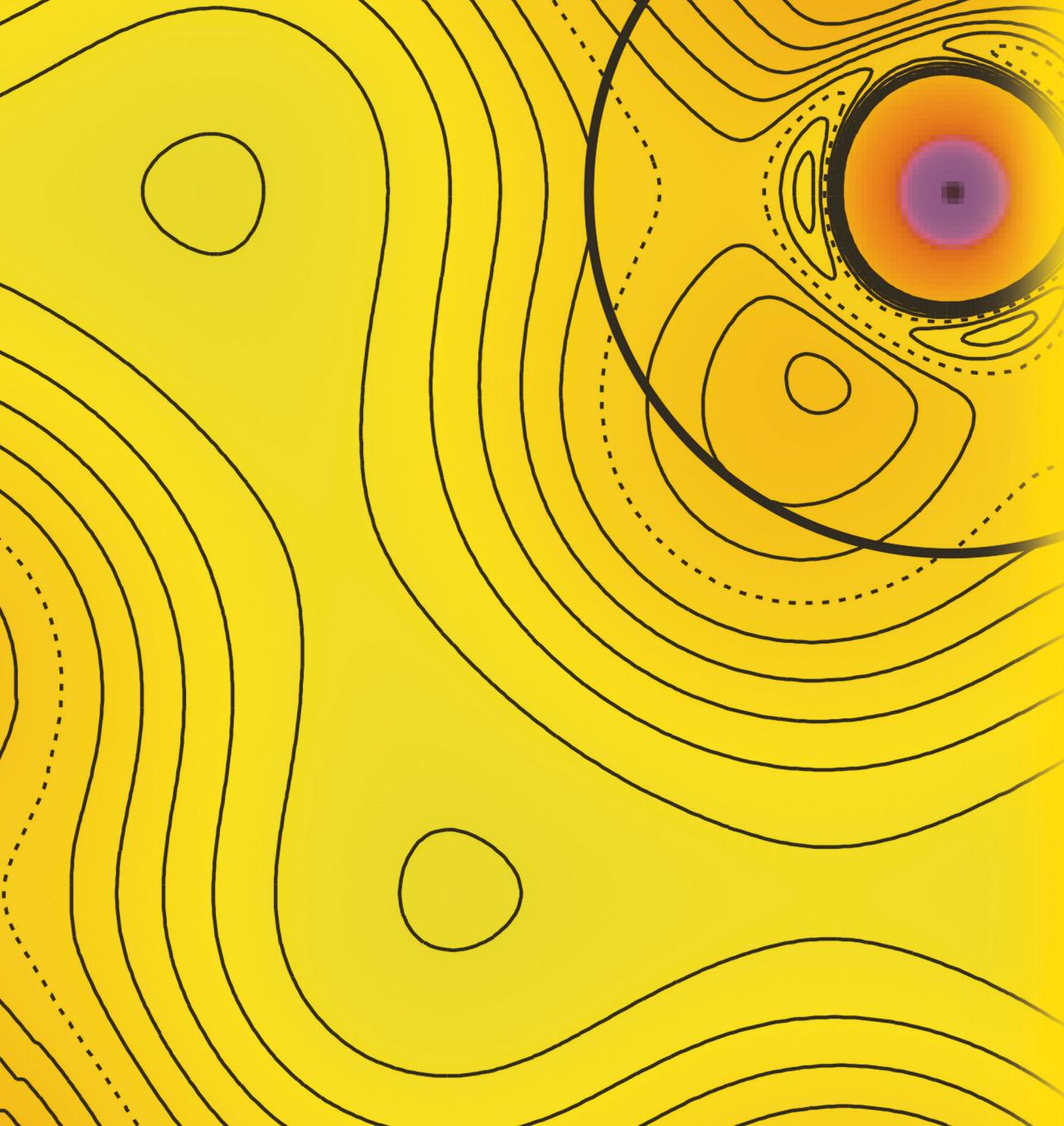
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