

**Heyd-Scuseria-Ernzerhof Screened-Exchange  
Hybrid Functional for Complex Materials:  
All-Electron Implementation and Application**

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# **Heyd-Scuseria-Ernzerhof Screened-Exchange Hybrid Functional for Complex Materials: All-Electron Implementation and Application**

Martin Schlipf

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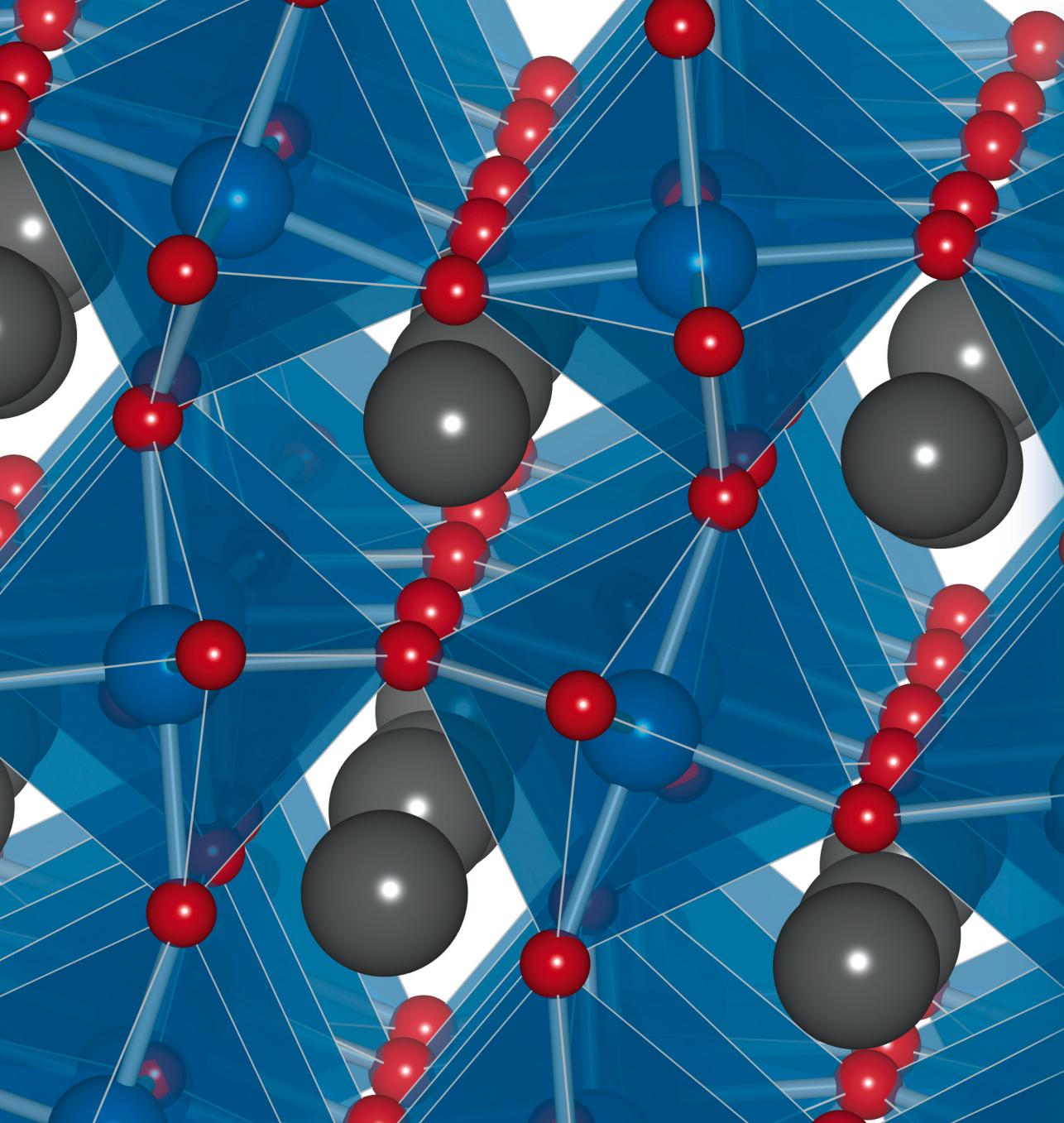
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