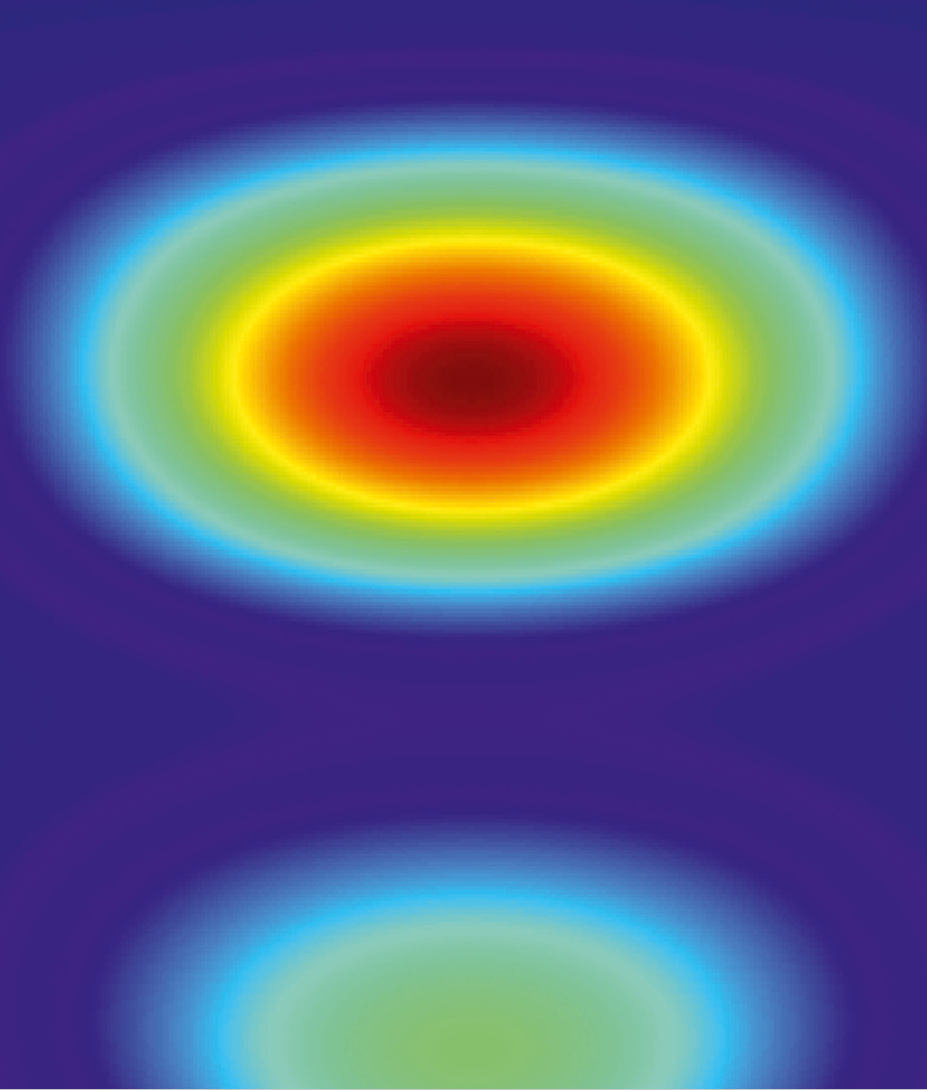




Single-Site Green Function of the Dirac Equation for Full-Potential Electron Scattering

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